# Autoranging CombiScope ${ }^{*}$ Instrument <br> PM3370B-PM3380B-PM3390B PM3384B-PM3394B 

MATH+ Users Manual
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## 1 INTRODUCTION

The MATHPLUS option gives your oscilloscope the added mathematical capability to make complex waveform measurements/decisions. For example, you can make "PASS/FAIL" measurements in an automated test environment, mathematically manipulate realtime and/or stored waveforms (addition, subtraction, multiplication, ....) , establish amplitude qualified cursors, and more.

This manual describes all mathematic functions that were described in the Users Manuals as well as additional mathematic functions and pass/fail testing.

In addition to the basic instrument functions described in the Users Manuals, Mathplus provides the following:

- Four more mathematical functions (integration, differentiation, fast Fourier transformation analysis, and histogram analysis).
- Probe scaling for scaling the input sensitivity and for presetting the dimension of the acquired trace.
- Pass/fail testing for testing waveforms against reference templates and calculated measurement results against preset limits. The action on a fail situation can be selected as beep, save, stop, or hard copy. A hard-wired output of the Fail condition is available.
- Measurement statistics to display additional statistic measurement results on the screen.
- Amplitude qualified cursors for timing measurements with time cursors automatically positioned relative to the signals: max peak, min peak, high level, or low level.
- Multiple-shot mode for capturing up to 200 ( 50 in 2 channel version) consecutive single shot acquisitions (if the memory extension installed).
- Varying the X POSITION of a stored trace allowing compensation for delay in measurement cables of different lengths.


## 2 MATHEMATICS

### 2.1 INTRODUCTION

Most oscilloscopes, including most Digital Storage Oscilloscopes, limit their capabilities to the display of amplitude (in volts), versus time. In addition to the traditional oscilloscope functions, the Autoranging CombiScopes ${ }^{\text {TM }}$ allow you to mathematically change the contents of each memory location. You can use the mathematics functions to calculate new waveforms from other traces that serve as input data.

The following section describes the mathematical functions implemented in your oscilloscope.

Note: The External Trigger input traces of the 2 channel versions can not be used as source for the mathematics functions.

The two mathematic functions (MATH 1 and MATH 2) are independent waveform processes. Both offer a choice of eight mathematical functions (add, subtract, multiply, filter, integration, differentiation, fast Fourier transformation analysis, and histogram analysis processes). These can be used in series or in parallel. The add, subtract, and multiply functions always require two source traces to operate; the other functions require only one source trace.

Acquired traces or stored traces can be used as source for mathematical operations and can be selected by using the $\Delta$ control in the ' MATH >> MATH 1' or 'MATH >> MATH 2' submenu. For best results, the source traces must be within the dynamic range of the scope. Inactive traces or empty memory locations cannot be used and the screen will display the message "INVALID SELECTION".

The result of MATH 1 is always stored in memory location ' m 1 '. The result of MATH 2 is always stored in memory location ' m 2 '. When used for mathematical functions, existing memory locations are overwritten. (Use the 'Copy' function to save important traces in another memory location, before using the mathematical functions.)

Independent operation enables separate processes to be performed at the same time. When the result of a mathematical function is placed in a register memory, functions can be chained together. An example is Ch1*Ch2, with the result being
integrated to measure power. In this example, MATH 1 is the multiply function with the product placed in m 1 and MATH 2 is the integration process, integrating the contents of m 1 , and placing the result in m 2 . The mathematical functions are performed on traces with differing units. Channel 1 shows volts over time, channel 2 shows current over time expressed in Ampères. The resulting trace of the multiplication fuction is expressed in Watts and gives the power over time. The units for the integrated trace are Joules.

Notes: - The mathematical functions give useful results only if there is no conflict between the units. For example, you cannot add ampères to volts.

- The trigger delay and the timebase setting of the two traces must be equal. This is always guaranteed if the traces were acquired at the same time (i.e., they are elements of the same register).


Figure 2.1 Example of chained mathematical functions

Note: $\quad$ Appendix A gives the complete menu structure of the MATH menu.

## Remote commands:

CPL: QW (Command to query a waveform).
Refer to the Operating Guide for full details

### 2.2 DEFINITIONS

An example that can be used with the formulas given below, the Probe Adjust signal was sampled and the trace data was sent to a personal computer using the RS-232-C serial interface and the Query Waveform command of CPL. The settings used and the most important elements of the response received were as follows:

| Settings | Attenuator <br> Coupling <br> Offset <br> Timebase <br> Delay | $\begin{aligned} & 200 \mathrm{mV} / \mathrm{div} \\ & \text { DC } \\ & -1.5 \mathrm{div}=-300 \mathrm{mV} \\ & 200 \mu \mathrm{~s} / \mathrm{div} \\ & -2.50 \mathrm{div}=500 \mu \mathrm{~s} \end{aligned}$ | ger view |  |
| :---: | :---: | :---: | :---: | :---: |
| Data | SYMBOL | PARAMETER | VALUE | TYPE |
|  | Yu | Y-units | V | string |
|  | Xu | X-units |  | string |
|  | Yz | Y-zero | 0.3 | number |
|  | Xz | X-zero | -0.0005 | number |
|  | Yr | Y-resolution | $3.125 \mathrm{e}-005$ | number |
|  | Xr | X-resolution | 4e-006 | number |
|  | Yrng | Y -range | 65535 | number |
|  | dT-corr | dT-correction | $4688 \mathrm{E}-04$ | number |
|  | N | sample count | 512 | number |
|  | Y[1] | sample 1 | 9603 | binary |
|  | Y [2] | sample 2 | 9612 | binary |
|  | Y[N] | sample N | -9599 | binary |

The following paragraphs give some definitions and formulas that enable you to interpret the preceding data. The same definitions, symbols, and formulas will be used to describe the discrete mathematical functions of the Mathplus processing functions.

Definitions You can describe a waveform using two one- dimensional arrays that contain wave sample information: $\mathbf{S}[1 \ldots \mathrm{~N}]$ and $\mathrm{T}[1 \ldots \mathrm{~N}]$. In both arrays the index " n " (range : 1...N) corresponds to the sample number. Data in the " S " array represents the amplitude of the waveform in volts of each sample, Data in the "T" array represents the sample time in seconds of each sample.

A waveform is sometimes expressed in other units. For example, an FFT waveform gives a range of frequencies (T[1]...T[N]; expressed in Hz ) for the signal amplitude of these frequency components (S[1]...S[N], expressed in dB).

## Formulas:

$\mathbf{S}[\mathrm{n}] \quad \mathrm{S}[\mathrm{n}]$ is the value of sample n , expressed in Y - units. Y -units are usually volts.

$$
S[n]=(Y z+(Y[n] \times Y r)) \times Y u
$$

Sensitivity Usually the sensitivity is expressed in volt/div. In the oscilloscope, the range of the $\mathrm{Y}[\mathrm{n}]$ values (Yrng) always equals $2^{\wedge} 16=65535$, which corresponds with 10.24 divisions on the screen. This gives a maximum vertical resolution of 6400 'levels' per division.
Sensitivity is expressed in Y-units/division.

$$
\text { Sensitivity }=6400 \times Y r \times \frac{Y u}{d i v}
$$

Offset Offset is the vertical screen position of the signal ground level, indicated by "1-" (excluding Y-pos shift). The offset can be adjusted with the front panel Y POS controls. For calculated traces, the offset can be adjusted with the delta controls in the MATHematics menu.
Offset is expressed in Y-units (volts).
Offset $=-Y z \times Y u$

NOTE: $\quad$ Traces can also be positioned with the $Y$-pos control in the RECALL menu, but this does not affect the offset. The reason is that $Y$-pos is a pure display function, which does not affect the signal sampling nor the calculation of a trace using a mathematics function.
$T[n] \quad T[n]$ is the sample moment, expressed in X-units. $X$-units are usually seconds.

$$
T[n]=(X z+(n-1) \times X r)+(d T-\operatorname{cor} r \times X r) \times X u
$$

Timebase In case of a sampled signal the horizontal scale is called the timebase. The timebase setting is usually expressed in seconds/ division. Without magnification or compression, the oscilloscope always displays 50 samples per horizontal division.

$$
\text { Timebase }=50 \times X r \times \frac{X u}{d i v}
$$

NOTE: $\quad$ The horizontal scale can differ, like the FFT scale. In this case it is expressed in X-units per division.

Delay The time delay between the trigger and the moment that the first sample is taken. If the delay is negative, the first sample is taken before the trigger. This is called pretrigger view. In pretrigger view, the trigger point (horizontal position of which $\mathrm{T}[\mathrm{n}]=0$ ) is indicated on the screen. The delay or the position of the trigger point can be adjusted with the TRIGGER POSITION control.
Delay is usually expressed in X -units (seconds).

$$
\text { Delay }=-(X z+(d T-\operatorname{cor} r \times X r)) \times X u
$$

$$
\text { Triggerposition }=(X z+(d T-\operatorname{cor} r \times X r)) \times X u
$$

These values can also be expressed in divisions:

$$
\text { Delay }=\left(\frac{-(X z+(d T-\operatorname{cor} r \times X r))}{X r}\right) \times \frac{1}{50} \times d i v
$$

$$
\text { Triggerposition }=\left(\frac{(X z+(d T-\operatorname{corr} \times X r))}{X r}\right) \times \frac{1}{50} \times d i v
$$

NOTE: The X-POS control in the RECALL menu can also be used to position traces horizontally, but this does not affect the delay or signal sampling because $X$-POS is purely a display function.

### 2.3 ADD

## Description:

The ADD function performs a point-to-point addition of two traces, related to the two ground levels (indicated as ' - '). The result of the ADD function is a new trace in a different register. The resulting trace can be scaled, and offset can be added for positioning.

NOTE: The front panel keys $\mathrm{CH} 1+\mathrm{CH} 2$ (or $\mathrm{CH} 3+\mathrm{CH} 4$ ) can also be used to display additional active traces of the sums of these channels. But you can use the mathematical ADD function even after a single shot or on stored traces.

Scaling is used to fit the resultant trace onto the screen. The TRACK control adjusts scaling.
Vertical positioning is called offset. It offsets each sample in the resultant trace with a value so that the trace can be "moved" vertically. The $\Delta$ control adjusts the vertical positioning.
The scale factor and the offset factor are displayed in the 'MATH SCALE' menu. Pressing the 'autoscale' softkey automatically selects the settings so the trace continues to fit onto the screen even if the input signals use the full dynamic range of the oscilloscope.

The amplitude settings are also used by the mathematical functions to obtain correct results if the settings of the two sources are different.

Either newly acquired traces or previously stored traces can be used as the sources for this process. The cursor controls are used to select sources. The resulting trace is automatically written into a register memory ( m 1 for math1 or m2 for math2).

To see the result more clearly, press the 'DISPLAY SOURCE on/off' softkey to turn off the two source traces.


Figure 2.2 Trace m1.1 is the result of the ADD function

## Mathematical description:

$S r=S_{1}+S_{2} \quad$ where Sr is the result

## Discrete mathematical formula:

$$
\operatorname{Sr}[n]=S_{1}[n]+S_{2}[n]
$$

For an explanation of the symbols, refer to Section 2.2.

## Key sequence:





DISPLAY
SOURCE
yes no

Control to select the ADD function.

Control to select the first source trace.

Control to select the second source trace.

Toggle softkey to switch the ADD function on or off.

Control to adjust the scale factor.

Control to adjust the offset factor.

Toggle softkey to select autoscaling.

Toggle softkey to switch the source
traces on and off.

### 2.4 SUBTRACT

## Description:

The SUBTRACT function performs a "point-from-point" subtraction of two traces, related to the two ground levels (indicated as ' - '). The result of the SUBTRACT function is a new trace in a different register. The resulting trace can be scaled and offset can be added for positioning.

NOTE: The front panel keys $\mathrm{CH} 1+\mathrm{CH} 2$ (or $\mathrm{CH} 3+\mathrm{CH} 4$ ) can also be used to display additional active traces of the subtraction of these channels. But you can use the mathematical SUBTRACT function even after a single shot or on stored traces.

Scaling is used to fit the resultant trace onto the screen. The TRACK control adjusts scaling.
Vertical positioning is called offset. It offsets each sample in the resultant trace with a certain value so that the trace can be "moved" vertically. The $\Delta$ control adjusts the vertical positioning.
The scale factor and the offset factor are displayed in the 'MATH SCALE' menu. Pressing the 'autoscale' softkey automatically selects the settings so the trace continues to fit onto the screen even if the input signals use the full dynamic range of the oscilloscope.

The amplitude settings are also used by the mathematical functions to obtain correct results if the settings of the two sources are different.

Either newly acquired traces or previously stored traces can be used as the sources for this process. The cursor controls are used to select sources. The resulting trace is automatically written into a register memory ( m 1 for math1 or m2 for math2).

To see the result more clearly, press the 'DISPLAY SOURCE on/off' softkey to turn off the two source traces.


Figure 2.3 Trace m1.1 is the result of the SUBTRACT function

## Mathematical description:

$\mathrm{Sr}=\mathrm{S}_{1}-S_{2} \quad$ where Sr is the result

## Discrete mathematical formula:

$$
\operatorname{Sr}[n]=S_{1}[n]-S_{2}[n]
$$

For an explanation of the symbols, refer to Section 2.2.

## Key sequence:





DISPLAY SOURCE yes no

Control to select the SUBTRACT function.

Control to select the first source trace.

Control to select the second source trace.

Toggle softkey to switch the SUBTRACT function on or off.

Control to adjust the scale factor.

Control to adjust the offset factor.

Toggle softkey to select autoscaling.

Toggle softkey to switch the source traces on and off.

### 2.5 MULTIPLY

## Description:

The MULTIPLY function performs a point-to-point multiplication of two traces. The value of each data point is related to ground. The result of the MULTIPLY function is a new trace in a different register. The resulting trace can be scaled, and offset can be added for positioning.

If the source traces are expressed in different units, the result will be automatically expressed in correct units. For example, a volt multiplied by an ampere will result in watts.

Scaling is used to fit the resultant trace onto the screen. The TRACK control adjusts scaling.
Vertical positioning is called offset. It offsets each sample in the resultant trace offset with a certain value so that the trace can be "moved" vertically. The $\Delta$ control adjusts vertical positioning.
The scale factor and the offset factor are displayed in the 'MATH SCALE' menu. Pressing the 'autoscale' softkey automatically selects the settings so the trace continues to fit onto the screen even if the input signals use the full dynamic range of the oscilloscope.

Either newly acquired traces or previously stored traces can be used as the sources for this process. The cursor controls are used to select sources. The resulting trace is automatically written in a register memory ( m 1 for math1 or m2 for math2).

To see the result more clearly, press the 'DISPLAY SOURCE on/off' softkey to turn off the two source traces.

One example of using the MULTIPLY function is the measurement of dissipated power, by taking the voltage across a device and multiplying it by the current through the same device. Refer to section 9.2 for an application example of multiplying a voltage trace and a current trace using the proper units.


Figure 2.4 Trace m1.1 is the result of the MULTIPLY function

## Mathematical description:

$S r=S_{1} \times S_{2} \quad$ where Sr is the result

## Discrete mathematical formula:

$$
\operatorname{Sr}[n]=S_{1}[n] \times S_{2}[n]
$$

For an explanation of the symbols, refer to paragraph 2.2

## Key sequence:



Control to select the MULTIPLY

DISPLAY
SOURCE

function.

Control to select the first source trace.

Control to select the second source trace.

Toggle softkey to switch the MULTIPLY function on or off.

Control to adjust the scale factor.

Control to adjust the offset factor.

Toggle softkey to select autoscaling.
Contol

Toggle softkey to switch the source traces on and off.

### 2.6 FILTER

## Description:

The FILTER function is a waveform MATH function. It is a post- acquisition algorithm that can be used for low-pass filtering or as display smoothing. The cutoff frequency of the low-pass filter can be adjusted and the resulting trace can be stored as a new trace in a separate register. This implies that the original waveform or trace is never disturbed by the process, allowing you to "experiment" with different filter factors.

A typical use of this digital low pass filter is to suppress noise even after a (single shot) acquisition. Since the FILTER function is a post acquisition process, it can also be used on single event waveforms.

Any newly acquired traces or previously stored traces can be used as sources for the filter process. The filtering is performed on all traces of a selected source register.
The resulting trace(s) are automatically written in memory location m 1 for math1 or m2 for math2 and are instantly displayed on the screen.

For each sample point of the trace, a weighed sum is calculated over a window of K samples (convolution). K is adjusted with the $\Delta$ control. The window width K is displayed in the 'MATH FILTER PARAM' menu. The resulting cut-off frequency is the result of the sample rate set by the timebase and the window. While the window is being adjusted, the -3 dB point is displayed in the bottom area of the screen.


Figure 2.5 Figure 2.5 Trace m1.1 is the result of the FILTER function

## Discrete mathematical formula:

$$
\operatorname{Sr}[n]=\sum_{\mathrm{k}=\frac{-(K-1)}{2}}^{\mathrm{k}=\frac{+(K-1)}{2}} S_{1}[n+k] \times F[k]
$$

where: $\quad \mathrm{K}$ is the window width (value may be between 3 and 41)
$k$ is the convolution index
$n$ is the sample point index
$F[k]$ is the filter function used for the convolution
The used filter function is given below. The sum of the components of the filter function is always 1 , so that the signal amplitude will not be affected.

$$
F[k]=\frac{1-\cos \left(\frac{\pi+2 \pi k}{(K+1)}\right)}{(K+1)}
$$

In case of a window width $K=3$, the filter values are:

$$
\begin{aligned}
& F[-1]=0,250 \\
& F[0]=0,500 \\
& F[1]=0,250
\end{aligned}
$$

For an explanation of the symbols refer to Section 2.2.

## Key sequence:



### 2.7 INTEGRATE

## Description:

The INTEGRATE function performs a numerical integration process on a trace. The horizontal area for the integration can be adjusted and the result is stored as a trace in a register. This trace can be scaled and positioned.

Scaling is used to fit the resultant trace onto the screen. Scaling is adjusted with the TRACK control.
Vertical positioning is called offset. It offsets each sample in the resultant trace with a certain value so that the trace can be "moved" vertically. The $\Delta$ control adjusts the vertical positioning.
The scale factor and the offset factor are displayed in the 'MATH INTEGR PARAM' menu.
Pressing the 'autoscale' softkey automatically selects settings that are optimal for typical applications as pulse power measurements.

Either newly acquired traces or previously stored traces can be used as the source for the integration process. The integration is performed on all traces of the selected source register, and the resulting traces are automatically written to a register memory ( m 1 for math1 or $m 2$ for math2) and instantly displayed on the screen.

The process can be done on a full trace, but also on a part of the trace (limited area). You can adjust the TRACK control for the left limitation and the $\Delta$ control for the right limitation. The AREA submenu also allows adjustment of the 'base line' used for the integration. Usually the base line is positioned at the GND level, but sometimes it is necessary to adjust the level because of offset of the input signal.

Two vertical cursors mark the trace interval related to the time; the horizontal cursor acts as an indication for the offset compensation. The cross sections of cursors are positioned at the result trace, giving a direct readout of the pulse power. Refer to paragraph 9.3 for an example that shows PROBE scaling (in amperes), MULTIPLY to measure power, and INTEGRATION to integrate pulse power.


Figure 2.6 Trace m1.1 is the result of the INTEGRATE function

## Mathematical description:

$$
S r(t)=\int^{t} S_{1}(t) d t
$$

o
were $\operatorname{Sr}(\mathrm{t})$ is the result

## Discrete mathematical formula:

$$
\operatorname{Sr}[n]=\sum_{\mathrm{k}=0}^{\mathrm{k}=\mathrm{n}}\left(S_{1}[n]-\left(-X_{1} z\right)\right) \times X_{1} r \quad \text { in } \mathrm{X}_{1} \mathrm{u} \times \mathrm{Y}_{1} \mathrm{u} \text { units }
$$

where: $\quad S_{1}[n]$ is the value of the source trace $-\mathrm{X}_{1} \mathrm{z}$ is the offset of the source trace, related to ground $k$ is the sample point index $X_{1} r$ is the horizontal resolution of the source expressed in X1u units

The formula can be expressed in the sample values ( $\mathrm{Y} 1[\mathrm{n}]$ in stead of $\mathrm{S} 1[\mathrm{n}]$ ) with the following conditions:

- The offset $(-Y r z)$ will initially be equal to the offset of the input trace $\left(-Y_{1} z\right)$, but may be adjusted with the offset control in the menu. This means that on screen, the ground marker of the source and result are initially positioned at the same level.
- The scale will have an initial value that is best for most applications. The scale is selected as a value in the 1-2-5 range and is related to the timebase setting and the sensitivity.
- The autoscale function sets the scale and offset factors back to the initial values.


## Key sequence:



Control to select the INTEGRATE function.

Control to select the source signal.

Toggle softkey to switch the INTEGRATE function on or off.

Control to adjust the scale factor.

Control to adjust the offset factor.

Toggle softkey to select the autoscaling.

Toggle softkey to switch area limitation on or off.

Control to adjust the left limitation

Control to adjust the right right limitation

Toggle softkey to switch the display of the source trace on or off.

### 2.8 DIFFERENTIATE

## Description:

The DIFFERENTIATE function performs a numerical differentiation process on a trace. The result is stored as a new trace in a different register. The result trace can be scaled and positioned.

Scaling is used to fit the resultant trace onto the screen. The TRACK control adjusts scaling.
Vertical positioning is called offset. It offsets each sample in the resultant trace offset with a certain value so that the trace can be "moved" vertically. The $\Delta$ control adjusts the vertical positioning.
The scale factor and the offset factor are displayed in the 'MATH DIF PARAM' menu.
Pressing the 'autoscale' softkey automatically selects preset values that are optimal for typical applications.

Either newly acquired traces or previously stored traces can be used as sources for the differentiation process. Differentiation is performed on all traces of the selected source register, and the resulting traces are automatically written in a register memory ( m 1 for math1 or m 2 for math2) and instantly displayed on the screen.

The menu allows adjustment of the window width (also called differential distance). The window selection adjustment and discrete mathematical formulas are described in the following paragraphs.


Figure 2.7 Trace m1.1 is the result of the DIFFERENTIATE function

## Mathematical description:

$$
\operatorname{Sr}(t)=\frac{d}{d t} \times S_{1}(t)=\frac{S_{1}\left(t+\frac{d T}{2}\right)-S_{1}\left(t-\frac{d T}{2}\right)}{d T}
$$

In the formula, dT is the differential distance, which can be selected in the menu. In theory, the smaller the dT, the more accurate the result. However, if the input signal is noisy, the result becomes even more noisy. The choice of dT setting, therefore, will depend on the input signal. The best setting is the smallest dT value that will output the most acceptable signal.

The used differential distance can be calculated from the number of samples in the window $(\mathrm{K})$ and the sample distance ( $\mathrm{Xr}=$ horizontal resolution).

$$
d T=(K-1) \times X r \quad \text { in Xu units; usually seconds }
$$

## Discrete mathematical formula:

$$
\operatorname{Sr}[n]=\frac{S_{1}\left[n+\frac{(K-1)}{2}\right]-S_{1}\left[n-\frac{(K-1)}{2}\right]}{(K-1) \times X r}
$$

expressed in $Y_{1} u / X_{1} u$ units
Where: n Is the sample point index
$\mathrm{K} \quad$ Is the window width
$S_{1}[n] \quad$ Is the value of sample $n$ of the source trace
$\operatorname{Sr}[\mathrm{n}] \quad$ Is the value of sample n of the result trace
The formula can be expressed in the sample values ( $\mathrm{Y} 1[\mathrm{n}]$ in stead of S 1 [ n$]$ ), with the following conditions:

- The offset (-Yrz) will initially be equal to the offset of the input trace $\left(-Y_{1} z\right)$, but may be adjusted with the offset control in the menu. This means that on screen, the ground marker of the source and result are initially positioned at the same level.
- The scale will have an initial value that is best for most applications. The scale is selected as a value in the 1-2-5 range and is related to the timebase setting and the sensitivity.
- The autoscale function sets the scale and offset factors back to the initial values.


## Key sequence:



DISPLAY
SOURCE


Control to select the DIFFERENTIATE function.

Control to select the source signal.

Toggle softkey to switch the DIFFERENTIATE function on or off.

Control to select the number of samples for the window.

Control to adjust the scale factor.

Control to adjust the offset factor.

Toggle softkey to select the autoscaling.

Toggle key to switch the display of the source trace on or off.

### 2.9 FAST FOURIER TRANSFORMATION (FFT)

## Description:

The FAST FOURIER TRANSFORMATION (FFT) function transforms an amplitude waveform from the time domain into the frequency domain. The resultant is a waveform, showing the power spectrum of the original trace. The horizontal axis of the FFT is the frequency axis; the vertical axis gives the amplitude of the frequency components found.
With the use of a high speed Digital Signal Processor (DSP), the complex waveform processing takes only a fraction of the time it would take on an average PC or on older measurement equipment.

Typical applications of FFT are in distortion tests, bandwidth and crosstalk measurements, signal purity analysis, and noise spectrum measurements.

The FFT function can be performed on any waveform in the acquisition system or in memory.
Both the source and the resultant waveform are single traces. The resultant trace is automatically written in either m1.1 (for math1) or in m2.1 (for math2) and is instantly displayed on screen.
Since the FFT process requires additional memory to store the 'imaginary' and 'real' parts of the FFT waveform, the oscilloscope must be set to an acquisition length up to 2 K (or 8 K when the extended memory option is installed). This is selected by TB-MODE, ACQ LENGTH, 4ch @ .. pts. These real and imaginary waveforms cannot be accessed by the user.

In general, any FFT algorithm assumes the source waveform is a representative part of a continuous, repetitive signal. As such, all signal components in the source signal should be described by a full number of cycles. During processing, the waveform memory content is repeatedly analyzed as if it represents different cycles. Thus any incomplete cycle results in a phase and amplitude jump in the waveform at the location where the beginning and the end of the memory content are supposed to come together (see figure 2.8).


Figure 2.8 Repeated waveform

This results in frequency components, called side-lobes, in the FFT display that do not really originate from the signal under test. To reduce this influence of incomplete cycles, different steps can be taken. These steps are known as 'windowing' and as 'zero filling' (see below).

## Horizontal resolution of FFT

The horizontal scale (frequency scale, in Hz ) of the FFT display depends on the setting of the timebase and the number of samples of the source trace. The standard setting for an acquisition record is 50 points per division. The minimum and maximum value of the scale can easily be calculated.

## Minimum frequency

The lowest frequency component ( $\mathrm{f}_{\text {min }}$ ) that can be discovered in a source trace, has a single period filling the entire acquisition record. This frequency can be calculated from the horizontal resolution (sample distance) of the source trace $(\mathrm{Xr})$ and the number of samples in a record N (acquisition length).

$$
\begin{aligned}
& X r=\text { Timebase setting } / 50=\mathrm{Tb} / 50 \\
& f_{\text {min }}=1 /(N \times X r)=50 /(N \times T b)
\end{aligned}
$$

## Maximum frequency

Every sinewave is defined by at least 2 points. So the highest frequency that can be determined in the FFT can be derived from Timebase (Tb);

$$
f_{\max }=(50 / 2) / \mathrm{Tb}=25 / \mathrm{Tb}
$$

Resolution
The resolution of the FFT is the smallest frequency step $\left(\mathrm{f}_{\mathrm{r}}\right)$ that can be made in a FFT result record containing $N$ samples. So the resolution gets higher when $f_{r}$ gets smaller.

$$
f_{r}=f_{\max } / N=(25 / \mathrm{Tb}) / N=25 /(N \times T b)
$$

This is half of the minimum frequency. Because the negative frequency component resulting from the FFT calculations is a mirror image of the positive ones, they can be omitted. So the positive side can be stretched over twice the area.

For a given timebase setting, the best possible frequency resolution can be obtained by selecting the longest possible acquisition record. With the Extended Memory option installed, record lengths up to 8 k can be used.

## Windowing

Windowing is a mathematical process that attenuates the parts of the waveform that are at the beginning and the end of the record.
As a result, the FFT is calculated mainly from the part of the record that is near the center. Thus incomplete cycles in the record have a reduced influence on the width of the sidebands of frequency components in the FFT.
The first and last samples have a reduced influence or no influence on the FFT. The window (FILTER) is selected in the MATHematics PARAMeter menu.

Rectangular window.
In fact, rectangular window equals no window. All samples are multiplied by 1.
Formula: $\quad$ sample $[n]=1 \times$ sample $[n]$

The major advantage of the rectangular window is its narrow main lobe. Using the rectangular window function provides the best frequency resolution.


Figure 2.9 Rectangular window

Hanning window.
The frequencies around the main lobe are considerably reduced compared to those passing through the rectangular window. The tradeoff for this lower noise floor is that the main lobe is wider. Therefore, you will not see frequencies close to the fundamental frequency.

Formula: $\quad$ sample $[n]=0,5 \times$ sample $[n] \times(1-\cos (2 \pi n / N))$


Figure 2.10 Hanning window

## Hamming window.

The main lobe is not as wide as it is with the Hanning window; therefore, the noise floor is a little higher. Frequencies closer to the fundamental can be seen without being drowned in noise.

Formula: $\quad$ sample $[n]=$ sample $[n] \times(0,54-0,46 \cos (2 \pi n / N))$


Figure 2.11 Hamming window

## Average

Average can be used to reduce the noise in the FFT result. This way more frequency components become visible.

## Zero filling

Zero filling is used when the LIMITED function in the MATHematics PARAMeter menu is turned on. The number of samples selected in the AREA menu is replaced by samples of the value zero. Thus, at baseline level, the waveform in memory can be reduced to a full number of cycles and a number of 'empty' samples. This is mainly useful when you are using the rectangular window. The other windows already reduce the effect of incomplete cycles.


Figure 2.12 Zero filling

## Cursor readout

There is only one cursor when the FFT result register is selected in the CURSORS menu. The cursor is used to find the frequency and the level of any component in the FFT result. Absolute or relative readout of the level is selected in the MATHematics PARAMeter. The dimension of the readout is selected in the CURSORS READOUT menu.

## Relative

The X -axis is a frequency domain. The Y -axis is a dB domain. Both scales are linear. Vertical scaling is always $10 \mathrm{~dB} / \mathrm{div}$. The top of the screen is always 0 dB . The frequency component with the largest amplitude is the reference $(0 \mathrm{~dB})$ for the other components. Changes in the source amplitude have no immediate effect on the FFT display.

## Absolute

The result of the FFT is processed to a power spectrum. The amplitude of the power spectrum is related to the amplitude of the input signal.

Power can be written as $P=U^{2} /$. So, for those cases where input and output impedance are the same, the output voltage can be expressed as a relation to the input voltage.

$$
d B=10 \log P_{2} / P_{1}=10 \log U_{2}^{2} / U_{1}^{2}=20 \log U_{2} / U_{1}
$$

However the dB does not automatically allow the expression of absolute levels. But, often a reference is made to a well known standard level, e.g., $1 \mu \mathrm{~V}$ or 1 mW . By doing so, absolute levels can be expressed as follows:

$$
\begin{array}{ll}
\mathrm{dB} \mu \mathrm{~V} & \mathrm{~dB} \text { with respect to } 1 \mu \mathrm{~V} \\
\mathrm{dBm} & \mathrm{~dB} \text { with respect to } 1 \mathrm{~mW}
\end{array}
$$

When you use dBm, you must know the impedance of the system to be able to convert from mV to dBm . The most common and often used impedances are 600 ohms (LF telecom) and 50 ohms (RF).

Note: This reference impedance selection does not imply that the input impedance of the oscilloscope is (or has to be) 50 ohm or 600 ohm.

Note: All voltage levels used in power calculations are in $V_{\text {rms }}$.
Reference level setting
The maximum displayed sinewave has an amplitude of 8 divisions p-p. This equals an amplitude of $8 / 2 \sqrt{ } 2=2.828$ div $_{\text {rms }}$. At $100 \mathrm{mV} /$ div, this equals $282 \mathrm{mV}_{\mathrm{rms}}$. Compared to 1 mW in 50 ohms ( 0 dBm ), this results in a reference level of 2 dBm .

Because 0 dBm on a graticule line is a much more convenient value for a reference, all values are recalculated to this 0 dBm at the top of the screen. This results in the reference levels in the table below.

| Attenuator |  | Reference level |  |  |
| :---: | :---: | :---: | :---: | :---: |
| setting | $\mathrm{V}_{\text {rms }}$ | dBm | dBm | $\mathrm{dB} \mu \mathrm{V}$ |
|  |  | @ 50 ohms | @ 600 ohms |  |
| $5 \mathrm{~V} / \mathrm{div}$ | 11.18 V | $+34 \mathrm{dBm}$ | 23.2 dBm | $141 \mathrm{~dB} \mu \mathrm{~V}$ |
| $2 \mathrm{~V} / \mathrm{div}$ | 4.47 V | + 26 dBm | 15.2 dBm | $133 \mathrm{~dB} \mu \mathrm{~V}$ |
| $1 \mathrm{~V} / \mathrm{div}$ | 2.24 V | + 20 dBm | 9.2 dBm | $127 \mathrm{~dB} \mathrm{\mu} \mathrm{~V}$ |
| 0.5 V/div | 1.12 V | + 14 dBm | 3.2 dBm | $121 \mathrm{~dB} \mu \mathrm{~V}$ |
| 0.2 V/div | 447 mV | + 6 dBm | - 4.8 dBm | $113 \mathrm{~dB} \mu \mathrm{~V}$ |
| $0.1 \mathrm{~V} / \mathrm{div}$ | 224 mV | 0 dBm | -10.8 dBm | $107 \mathrm{~dB} \mu \mathrm{~V}$ |
| $50 \mathrm{mV} / \mathrm{div}$ | 112 mV | -6 dBm | - 16.8 dBm | $101 \mathrm{~dB} \mu \mathrm{~V}$ |
| $20 \mathrm{mV} / \mathrm{div}$ | 44.7 mV | - 14 dBm | - 24.8 dBm | $93 \mathrm{~dB} \mu \mathrm{~V}$ |
| $10 \mathrm{mV} / \mathrm{div}$ | 22.4 mV | - 20 dBm | - 30.2 dBm | $87 \mathrm{~dB} \mu \mathrm{~V}$ |
| $5 \mathrm{mV} / \mathrm{div}$ | 11.2 mV | - 26 dBm | - 36.2 dBm | $81 \mathrm{~dB} \mu \mathrm{~V}$ |
| $2 \mathrm{mV} / \mathrm{div}$ | 4.47 mV | - 34 dBm | - 44.2 dBm | $73 \mathrm{~dB} \mu \mathrm{~V}$ |

Other reference impedances
For other reference impedances X , a correction factor $\mathrm{C}_{\mathrm{x}}$, can be calculated and added to the $\mathrm{dBm} @ 50$ ohm table.

$$
C_{x}=20 \log \sqrt{(50 \mathrm{ohm} / \mathrm{X} \mathrm{ohm})}=10 \log 50 / X
$$

e.g. $75 \Omega \quad C_{75}=10 \log 50 / 75=-1,76 d B$

So if a signal was measured in a 75 ohms system at +20 dBm where the measerement was based upon a 50 ohms system, the actual signal is then $+20 \mathrm{dBm}-1.76 \mathrm{dBm}=+18.24 \mathrm{dBm}$.


Figure 2.13 FFT reference level

## Key sequence:



Control to select the FFT function.

Control to select the source signal.

Toggle softkey to switch the FFT function on or off.

Toggle softkey to switch the area limitation on or off.

Control to adjust the left limit.

Control to adjust the right limit.

Toggle softkey to select a FFT window.

Toggle softkey to select absolute or relative cursor readout.

Toggle key to turn the display of the source trace on or off.


Softkey to turn the cursors off.

Softkey pair to select the source register for cursor readout. Memory location m 1.1 is the result register of the MATH1 function, and m2.1 the result register of the MATH2 function.

Softkey pair to select the dimension of the cursor readout result.

Toggle softkey to select the reference impedance of 50 ohms or 600 ohms.

### 2.10 HISTOGRAM

## Description:

The HISTOGRAM function calculates an amplitude density graph of a trace.
Typical use of the histogram function is data transmission, e.g., in telecommunication.

The result of the histogram function is a new trace in a different register. The new trace is automatically scaled between -2 and +3 divisions.

Either newly acquired traces or previously stored traces can be used as the source for the histogram process. The result and the source are a single trace. The resulting trace is automatically written as the first trace in a register memory ( m 1.1 for math1 or m2.1 for math2) and is instantly displayed on the screen.

In the histogram the horizontal axis represents the voltage levels (called 'classes'). The vertical axis represents the number of times each voltage level was present in the source trace. (The number of occurrences is sometimes also called density.) The result is always presented with a resolution of 512 'classes' and is put into the first 512 samples of a trace.


Figure 2.14 Trace m1.1 is the result of the HISTOGRAM function

If cursors are used, only one cursor is displayed; it shows a marker on the crossing point of the resulting trace. The corresponding density is then displayed in the top area of the screen (expressed in \%).

NOTES: - If averaging is not used, the result will effectively contain only 256 classes, which is equal to the ADC resolution (2^8bit).

- If the trace length of the source is higher, the vertical resolution of the result will increase. The more samples that are taken, the higher the accuracy of the statistics.
- The calculation of a histogram requires a lot of memory; therefore, the histogram function cannot be performed in the 4 K and 8 K modes (or in the 16 and 32 k modes if the memory expansion option is installed). The .2 .3 and . 4 traces of the result trace are used by the calculation algorithm.


## Key sequence:



Control to select the HISTOGRAM function.

Control to select the source signal.

Toggle key to switch the HISTOGRAM function on or off.

Toggle key to switch the display of the source trace on or off.

## 3 PROBE SCALING

## Description:

The 'UTILITY PROBE SCALE menu' has been expanded in the Mathplus option. This menu now offers the capability of probe scaling and can be used for the mathematic functions.
This menu is reached via the key sequence: ‘UTILITY >> PROBE >> PROBE CORR >> SCALE'.

For each channel (incl. EXT TRIG on 2 channel models) you can select a scale factor and the unit.
The following units can be selected: V (volts), A (amperes), $\Omega$ (ohm), W (watt), J (joule), C (degrees centigrade), K (kelvin), P (pascal), m (meter) or U (unit). The scale factor is a floating-point value with an exponent, and can be selected with the $\Delta$ control. Cursor readouts, mathematics and measurements, are performed and displayed in the proper units.

When performing mathematical processes to one or two signals, the instrument automatically adapts the unit and exponent of the new trace type.

Example: A current (A) is applied to Ch1, and a voltage ( V ) is applied to Ch2. The resulting trace of the multiply function will automatically have a ' $W$ ' indication as unit. After integration the result will be the energy and will be expressed in joule (J).

The 'scale on/off' softkey sets the predefinition for all channels on or off.

## Key sequence:



Softkey pair to select for which channel the probe scaling is valid.

Control to adjust the scale factor for the selected channel.

Control to adjust the unit for the selected channel.

## 4 PASS/FAIL TESTING

## Description:

In addition to the basic measurements (MEAS1 and MEAS2), the MEASURE menu has been expanded with a PASS/FAIL testing facility. This allows you to test waveforms against reference templates (envelope) and calculated measurement results against preset limits. The screen displays the result of the test (PASS or FAIL). The action on a fail situation is user selectable. The action can be beep, save, stop, and hard copy. The scope also provides a hardware output. Pass/fail testing is very useful for semi-automated test applications (ATE). No visual interpretations of displays are needed.

To enter the pass/fail testing mode, select 'PASS/FAIL' from the MEASURE menu. The menu displays the choices, and you use a softkey to select the TEST menu or the ACTION menu. Pressing the 'on/off' softkey switches off the menu again, and you can activate the pass/fail action by pressing the 'run/stop' softkey (run activated).

## Pass/fail test

You can select one of the four pass/fail TEST modes: envel, meas1, meas2, or cursor.

## - Envel

Envelope pass/fail testing can be used for comparing a waveforms against a reference template (envelope). Either newly acquired traces or previously stored traces can be used as reference waveforms. Adjust the $\Delta$ control to select the source waveform. When the test trace exceeds the limits of the template during testing, the scope will act as selected in the 'ACTION' menu.


Figure 4.1 Create envelope for pass/fail testing

Envelope pass/fail testing cannot use the External Trigger channel or its memory location (mx.e) in the 2 channel versions. When you acquire the reference waveform in the envelope mode, you can use it directly as a template. When you need a user- defined template, select the 'EDIT ENVELOPE' softkey to enter the edit mode. In this menu you use a horizontal shift softkey pair and a vertical softkey pair to define the envelope from the selected source waveform. When you use a trace from a protected register memory, the EDIT CONFIRM menu is activated first to overrule the register protection.

A second option is to draw a template without the use of a source trace. Then press the 'DRAW' softkey to enter the DRAW ENVELOPE mode. The envelope register must be cleared first. This is done in the DRAW CONFIRM menu that is displayed when necessary.
In the DRAW ENVELOPE menu you can draw the upper and lower limit of the template by turning the TRACK control and $\Delta$ control to find the VERT POS and HOR POS of the selected limit. One horizontal and one vertical cursor display the two positions and the crossing of the two cursors mark a point on the template. Press the CONNECT softkey to define the first point and continue with ACCEPTing next points until the template is completed.

If necessary you can store and protect entire libraries of templates (for example, the CCITT standardized masks) in the internal register memory of the oscilloscope.

## - Meas1

Pass/fail testing is done by comparing the calculated results of measurement 1 against preset limits. To enter the defined test range mode, select 'RANGE' from the DEFINE TEST menu. The menu now displays the choices, and you use a softkey to select one of the three following test range modes:
>limit gives a fail condition for all values higher than the selected limit. You adjust this limit with the TRACK control.
<limit gives a fail condition for all values lower than the selected limit. You adjust this limit with the TRACK control.
range gives a fail condition for all values outside the selected range. You adjust the upper limit with the TRACK control, and the lower limit with the $\Delta$ control.

## - Meas2

Pass/fail testing by comparing the calculated results of measurement 2 against preset limits.

## - Cursor

Pass/fail testing is done by comparing a cursor readout against preset limits. The cursor readout to be tested can be selected :
$\Delta \mathrm{V} \quad$ the voltage difference between the cursors.
V1 the absolute voltage with respect to ground.
$\Delta T \quad$ the time difference between the cursors.
$1 / \Delta \mathrm{T}$ the calculated frequency.

To enter the 'define test range mode', select 'RANGE' from the DEFINE TEST menu. The menu now displays the choices, and you use a softkey to select one of the three test range modes:
>limit gives a fail condition for all values higher than the selected limit. You adjust this limit with the TRACK control.
<limit gives a fail condition for all values lower than the selected limit. You adjust this limit with the TRACK control.
range gives a fail condition for all values outside the selected range. You adjust the upper limit with the TRACK control, and the lower limit with the $\Delta$ control.

The pass/fail testing on cursors is very useful in combination with the Amplitude Qualified Cursor mode. Refer to Chapter 6.

## Pass/Fail Action

The action on a fail situation can then be off, beep, stop, save, or hard copy. To enter the Pass/fail action mode, select the 'ACTION' softkey from the PASS/FAIL TESTING menu. The menu now displays the choices, and you use a softkey pair to select one of the following actions in a fail conditions:


Figure 4.2 Waveform: pass/fail

- off No reaction on a fail condition.
- beep An audilbe signal warning of a fail condition.
- stop Stop of signal acquisition; the screen displays the "fail trace". This mode can be used to automatically capture the first violating waveform.
- save The "fail trace" is automatically written in a selected register memory location. The TRACK control selects the register memory. Memory locations reserved for External Trigger View signals (mx.e) cannot be used. Of course, the destination register memory may not be protected if it is used to save the fail waveform. The save mode is used to automatically store the latest (most recent) fail situation.
- hcopy A hard copy of the "fail trace" is made to a printer or a plotter.

In addition to one of the five fail actions, pin 4 of the RS- 232-C output connector can become LOW on a fail condition. You must then set the 'HW-OUT yes/no' menu selection to 'yes' and you must also select ' 3 -wire' in the UTILITY >> RS232 SETUP menu. You can use this line to control an external device.

## Key sequence:

Envelope testing:


Measure testing:


Toggle softkey to switch pass/fail testing on and off.

Softkey pair to select measure testing.

Toggle softkey to switch between >limit, <limit or range condition for testing.

Control to adjust upper limit.

Control to adjust lower limit.

Softkey to activate the ACTION menu; see below.

Toggle softkey to start the pass/fail testing.

Cursors testing:


Toggle softkey to switch pass/fail testing on and off.

Softkey pair to select cursor testing.

Softkey pair to switch between $\Delta \mathrm{V}, \mathrm{V} 1, \Delta \mathrm{~T}$, or $1 / \Delta \mathrm{T}$ readout.

Toggle softkey to switch between >limit, <limit, or range condition for testing.

Control to adjust upper limit.

Control to adjust lower limit.

Softkey to activate the ACTION menu; see below.

Toggle softkey to start the pass/fail testing.

Action menu:


Toggle softkey to switch pass/fail testing on and off.

Softkey pair to switch between off, beep, stop, save, or hardcopy action after fail condition.

## Remote commands:

CPL: PW (Command to program a waveform) QW (Command to query a waveform)
Refer to the Operating Guide for full details.

## 5 MEASUREMENT STATISTICS

## Description:

In a standard oscilloscope you can perform two calculated measurements (MEAS1 and MEAS2). Once selected, the actual value of the measurement is instantly displayed in the top left corner of the screen. This measurement can be done on newly acquired traces or on stored traces. In 2 channel models only the input channels or their stored traces can be measured.

When you set the MEASURE >> STATIST menu selection to 'on', the screen displays three more values. These values are measured over the total number of acquisitions for that particular measurement and is updated instantly.

The additional statistic measurement values are as follows:

- absolute minimum value.
- absolute maximum value.
- mean value.

NOTE : When you use the statistic measurement in pass/fail testing, the testing is done on the mean value of the trace instead of the actual value.

## Key sequence:



Toggle softkey to switch the statistic measurement on and off.

## 6 AMPLITUDE QUALIFIED CURSORS

## Description:

The standard instrument is provided with two independent cursors that can be positioned on newly acquired signals or on previously stored traces. By using the cursors you can make fast and accurate amplitude (=), time (\|), or both amplitude and time (\#) measurements in digital and analog mode. You find a full description of these basic cursors functions in the Operating Guide.

The Mathplus option allows you to use amplitude qualified cursors. These enable highly automated timing measurements with time cursors automatically being positioned relative to the displayed traces. This is very useful for rise time measurements on signals with aberrations, measurements on a specific pulse in a pulse train, or various pulse width measurements.

The amplitude qualified cursors are activated with the key sequence 'CURSORS >> auto >> ...'. The cursor controls let you locate the horizontal cursors relative to reference levels ( $0 \%$ and $100 \%$ ). These reference levels are displayed on the screen as dotted lines. The cursors then search horizontally for the point where the trace crosses the cursor level, and the cursors are positioned at these points. You can determine the condition of the cursor searching using the 'SEARCH' submenu. The cursor readout is at the top of the screen.

The 'SEARCH' feature enables you to find the $n$-th occurrence ( $n=1,2,3$ or Last) of the two amplitude qualified cursors independently. This allows you to measure on a specific pulse in a pulse train.

You can set each of the four reference levels for the amplitude qualified cursors (C1-0\%, C1-100\%, C2-0\%, and C2-100\%) using the 'CURSORS SEARCH REF's' menu. The options that can be selected are :

- min the most negative trace value.
- max the most positive trace value.
- high the voltage level that corresponds with the top flat part of the trace. This eliminates the influences of overshoot or ringing on time measurements.
- low the voltage level that corresponds with the bottom flat part of the trace. This eliminates the influences of undershoot or ringing on time measurements.
- gnd the ground level, indicated by "-".
- abs the absolute voltage level. The TRACK control adjusts the level for the selected cursor. The menu displays this level.

Initially the readouts in the top text area are displayed in relative values (\%). But you can press the READOUT softkey to change to absolute values (usually volts).

For optimum visibility of trace detail, press the 'DISPLAY REF's on/off' softkey to turn off the reference cursors.


Figure 6.1 Measuring the width of a burst of pulses


Figure 6.2 Measurement of recovery time from overshoot

## Key sequence:



Toggle function softkey to switch between cursors on and off.

Toggle function softkey to switch between volts, time, mixed or amplitude qualified cursors.

Toggle function softkey to select the occurrence of cursor C1.

Toggle function softkey to select the occurrence of cursor C2.

Toggle function softkey to switch between relative or absolute readouts.

Softkey pair to select between the cursor conditions. This can be done for all four reference conditions. If 'abs' is selected, the TRACK control adjusts the level.

Toggle function softkey to turn the reference cursors on and off.

## Remote commands:

CPL:QM (command to query measured values)
Refer to the Operating Guide for full details.

## 7 MULTIPLE SHOT

## Description:

The MATHPLUS option offers in addition to the three basic timebase modes (AUTO, TRIG, and SINGLE) the MULTIple shot mode. The mode selection is done in the TB MODE menu.

Multiple shot enables the 4 channel instruments, to perform up to 32 (200 for extended memory) consecutive single-shot acquisitions. The 2 channel instruments allow up to 16 ( 50 for extended memory) consecutive single-shot acquisitions. Pressing the SINGLE key resets the scope for single-shot operation; the trigger level is set to 0.5 division (indicated by T-). You can now select singleshot or multiple-shot mode in the TB MODE menu. From now on, the selected mode is used every time the SINGLE key is pressed.

In the multiple-shot mode, the acquisition is stored in the highest unprotected memory location. The scope then automatically rearms for the next acquisition and stores it in the memory location with the next lower index. This continues until the whole memory is filled or a protected memory location is met. Depending on the number of active channels and the selected memory configuration (acquisition @512, @2K,...), a single register can contain 1, 2, or 4 shots.

## Key sequence:



SINGLE


Softkey pair to select between the timebase modes including multiple shot.

Key to reset the MAIN TB in multiple-shot mode, with ARM'D indicator.

## 8 VARYING X POSITION

## Description:

You can display previously stored traces at any time and in any combination. When you recall multiple traces, the standard instrument version allows you to vary the Y-POSition of a displayed stored register (e.g., m4) or trace (e.g., m4.1). This is done with the $\Delta$ control in the 'RECALL REGISTER MEMORY' menu

When the Mathplus option has been installed, you can also vary the X-POSition of a displayed stored trace. To enable this control, press the bottom softkey in the RECALL REGISTER MEMORY menu and select 'trace' mode. Then select either Y-POS or X-POS from the 'RECALL REGISTER MEMORY' menu to define the function of the $\Delta$ control. A softkey selection in the 'RECALL REGISTER MEMORY' menu defines the function of the $\Delta$ control, whether used for Y-POS or for X-POS.

The X-POS feature is useful for observing and comparing stored traces that are time related and for delay compensation of measurement cables of different length.

## Key sequence:



Toggle softkey to select out of the trace or out of registers.

Control to select the traces to recall.

Toggle softkey to turn the selected traces on or off.

Softkey to define the $\Delta$ control as X-POS control.

Control to horizontally shift the selected recalled trace.

## 9 APPLICATIONS

### 9.1 INTRODUCTION

Oscilloscopes have always enabled the electronics engineer to view electrical signals. Up to now, this is usually limited to showing voltages measured in a system.

The Autoranging CombiScope family of oscilloscopes can do many mathematical operations, so that you can derive information from measurements that is not obvious to see in the original traces.
This chapter gives examples of this mathematical processing, and provides the explanation of how this type of processing expands the measurement capabilities of the oscilloscope.

### 9.2 POWER MEASUREMENT

Oscilloscope measurements can be made of voltage or current, then circuit or device power can be calculated from these measurements.
But, the Autoranging CombiScope family of multichannel oscilloscopes can simultaneously measure both voltage and current and multiply waveforms, thus calculating and displaying electrical power as a function of time.
This measurement will be reliable over a wide range of frequencies, irrespective of the wave shapes of voltage and current. These measurements can be used in systems equipped with switching components such as switch mode power supplies where power can be a critical factor.
In Figure 9.1a, an ac voltage source V1 is loaded by a resistor Rload. This causes current (I) to flow in the system.

Figure 9.1 Basic set-up for Power Measurement


In Figure 9.2 a copy of the original oscilloscope screen is shown with part of the instruments setup information. The figure shows both signals: channel 1 (ch1) shows voltage V 1 at a vertical deflection setting of $5 \mathrm{~V} /$ div (volts per division), channel 2 (ch2) shows the current. The channel 2 deflection setting is indicated as $0.2 \mathrm{~A} / \mathrm{div}$ (amperes per division). This is achieved by changing the probe scaling of channel 2 to adapt for an external current-to-voltage conversion, giving one volt output per ampere input.
The conversion itself was achieved by placing a $1 \Omega$ measurement resistor Rm in series with the load and applying the voltage across this series resistor (see Figure 9.1b) as V2 to oscilloscope channel 2 (ch2).

Refer to Figure 9.2; it appears V 1 (ch1) has an amplitude of 5.5 Vp , the current has a peak value of 222 mA .
The oscilloscope was set up to multiply this waveform information and to store the resultant waveform in memory 1 as channel 1 (m1.1).


Figure 9.2 Oscilloscope screen showing the voltage (ch1) and current (ch2) waveforms together with the momentary power curve (m1.1)

NOTE: Multiplication at the ch1 and ch2 waveforms results in the center waveform displaying the momentary power. Cursor measurement on this power curve shows the peak power in the resistor is 1.27 Watts.

Use the following key-sequence to activate this multiplication process:

- Enter the MATH menu.
- Select MATH 1, m1 = >.
- Turn the TRACK control to select the multiplication operation to select ch1 and ch2.
- Press ENTER and turn on the mathematical operation.
- Change the display size and position if necessary.


## Scaling and Scale factor

If the measurement resistor Rm has a value other than $1 \Omega$, the current-to-voltage conversion ratio can be used for the scaling factor according to the following formula:

SCALEfactor $=\frac{1}{R m}$

Example: Suppose a current of 2 amperes is flowing in the system. This current will cause a 2 -volt signal across a 1 ohm resistor. If an oscilloscope with a vertical deflection setting of $1 \mathrm{~V} / \mathrm{div}$ is used to measure this, the deflection indication of the oscilloscope should be 1 A /div instead of $1 \mathrm{~V} /$ div; signal amplitude will be 2 divisions. If the resistor is replaced by a $0.5 \Omega$ type, the voltage across it will be just 1 volt, giving a signal amplitude on screen of 1 division. The scaling factor should be set to 2.000 E00 to get a current reading of $2 \mathrm{~A} / \mathrm{div}$.

Use the following key sequence to change the readout of channel 2 to indicate A/div (amperes per division):

- Enter the UTILITY menu.
- Select PROBE >, PROBE CORRection >, SCALE > and select this function to work on channel 2 , switch it ON.
- Use the $\Delta$ control to select another unit of measure for the channel 2 deflection factor, select UNITS A (= amperes).


### 9.3 INTEGRATION OF A WAVEFORM

The mathematical process of integration can be seen as the summation of all signal values of a waveform over time. In a sampled system like an oscilloscope, this comes down to the summation of all individual samples, including signs, over time. This allows you to measure the accumulated effect over time of individual events or individual parts of a signal. The resultant waveform expresses V *s (voltseconds) as a function of time if the original curve is in volts per division or expresses Coulomb if the source waveform is in Amperes per division.
Applications include measuring the charge stored in a device, being the integrated waveform of the current, measuring the dissipation as the integrated curve of power, and many more.

In Figure 9.3, channel 1 shows a current step of 8.92A that is used to charge a capacitor (ch1). As a result, the charge in the capacitor will increases linearly. Mathematical operation 2 is used to integrate the current waveform, resulting in a curve ( m 2.1 ) that represents the charge stored in the capacitor.

The vertical deflection of the processed curve has been set to give a scaling of $25 \mu \mathrm{C} / \mathrm{div}$ (micro-coulombs per division).
The cursors were used to measure the charge stored is $141 \mu \mathrm{C}$ per cycle.

PMЭ394, FLUKE


Figure 9.3 Waveforms showing step current (ch1) and charge stored in the capacitor (m2.1)

Key sequence is:

- Enter the MATH menu
- Press MATH 2
- Enter MATH 2 m2 = > and use the TRACK control to select the integration process.
- Use the $\Delta$ control to select the acquisition as the source for the mathematical process and press ENTER.
- Set the on/off toggle to ON.
- Enter the PARAMeter submenu to change the vertical deflection setting to $25 \mu \mathrm{C} / \mathrm{div}$ or its position (OFFSET).
- Enter de CURSOR menu, select vertical cursors on m2.1, enter the READOUT submenu and switch over the $\mathrm{V} 1 \& \mathrm{~V} 2$ readout.


### 9.4 POWER MEASUREMENT IN A SWITCH MODE POWER SUPPLY

The size and weight of electronic equipment is often dominated by the size and weight of the power supply it incorporates, so switch mode power supplies (SMPS) are used to make products smaller and more lightweight.
Because the size and weight of these power supplies in turn depends on their operating frequency, much effort is spent increasing the converter's frequency of operation.

The losses in efficiency due to the switches are the main limitation to this increase in frequency. Measurement of the losses is therefore of crucial importance in the design of SMPS.

In Figure 9.4, the power stage of a flyback type SMPS is shown. During the forward stroke, the transistors V1 and V2 conduct and charge the transformer, and increase the current through the transformer's primary winding. This causes the voltage across Rm to increase until it is high enough to fire V3. This switches off V1 and V2 for the duration of the flyback stroke, and forces the transformer to discharge via the secondary windings of the transformer.


Figure 9.4 Power stage of a Switch Mode Power Supply

Losses occur mainly in the switcher components V1 and V2 due to their switching speed and are mainly during the phase where the transistors are switched on again. At that time the voltage over the transistors is high, and the current starts to increase.
These losses can easily be measured by applying the collector voltage of V2 and the voltage across Rm to the oscilloscope (see Figure 9.5).


Figure 9.5 SMPS voltage (upper trace) and current waveforms


Figure 9.6 Momentary Power as a function of time

The oscilloscope is used in the windows mode, that is, the two source traces are each displayed over half the vertical size of the screen (four divisions), thus giving an optimal use of the screen and good separation of the two traces while maintaining high vertical deflection settings. The vertical deflection readout is adapted to the new waveform display size.
Figure 9.6 shows the mathematically obtained resultant waveform; the measurements indicate the maximum peak is approximately 98.2W.
Also a negative (and much larger) peak can be seen in Figure 9.6. This peak corresponds to the power handled by the flyback diodes at the moment the flyback stroke starts. Since at that moment voltage and current are of opposite sign, a negative value is found. This negative sign indicates that the current does not go through the transistors. This power peak is therefore not handled by the
transistors and needs not to be taken into account where the power handling of the transistors is concerned.

The key-sequence to set up the oscilloscope for this power curve calculation is as follows:

- Attache probes measuring the collector voltage and the output current to the oscilloscope channels 1 and 2.
- Set the probe scaling for the current measurement on the appropriate channel.
- Enter the UTILITY menu.
- Select PROBE > and PROBE CORRection >.
- Select the channel that represents the current (here ch2).
- Press SCALE > and change the units into A (amperes) by using the $\Delta$ control and adapt for the value of the measurement resistor Rm by setting a SCALE factor equal to ( $1 / \mathrm{Rm}$ ) with the TRACK control. Notice the vertical deflection indication changes according to the scale factor and units of measure used.
- Enter the MATH menu, select MATH 1, set up the mathematical operation 1 for multiplication using the TRACK control and select ch1 and ch2 as the source waveforms by means of the $\Delta$ control.
- Press ENTER and switch on (on/off) the mathematical operation. Now the SCALE sub-menu can be entered if the resultant waveform has to be changed in vertical size or offset (position).

Perform the following steps to measure the peak power:

- Select the MEASURE menu.
- Select measurement 1 and toggle the first softkey until the 'volt' mode is highlighted.
- Use the TRACK control to measure the MAXimum peak.
- Use the $\Delta$ control to do the measurement on m1.1.
- Press RETURN and switch on measurement 1.

MINimum peak can be measured in the same way as MEAS 2 to indicate the power peak handled by the diodes.

### 9.5 PULSE POWER OR DISSIPATED ENERGY MEASUREMENT

The power the transistors handle is converted into heat. The risk of damage to a component depends on the peak power that the component handles, and also on the total dissipation of the component. Too much dissipation will cause the temperature of the device to be too high.
The dissipation is proportional to the integral of the power curve over time.

The dissipation in the transistor takes place during the conducting phase (where the transistor is carrying current) and during the switching transitions. In Figure 9.7 was zoomed in on that part of the waveform of Figure 9.6.


Figure 9.7 Power handling by the devices during the conducting phase of the SMPS

The power curve was derived from part of the signal and used as the source for an integration process.
The integrated waveform shows the accumulated pulse power, dissipated by the devices.
The cursors can be used on this waveform and give a read-out in joules (J), which is the equivalent of Ws (watt-seconds).
In order to know the total dissipation of the devices per second, we have to multiply the dissipation per cycle, which was found to be $175 \mu \mathrm{~J}$, and the number of cycles per second ( 33.7 KHz , see figure 9.5) and find 5.9 W .

Once the instrument makes the power curve (described in the previous paragraph), the following key-sequence can be used to come to the integrated curve:

- Enter the MATH menu.
- Select MATH 2.
- Select MATH $2 \mathrm{~m} 2=>$.
- Select the integration operation by using the TRACK control.
- Use the $\Delta$ control to select the result of MATH 1 in memory 1 as the source for the operation.
- Press ENTER, switch the processing function on. If desired, select from the PARAMETER menu to change the offset of the curve or select a different vertical scaling for the resultant curve.

The integration process can also be performed in a limited area, that is, part of the source waveform can be neglected by indicating the process has to be performed over a limited area only. If you select this function is selected by setting 'LIMITED yes', a new AREA submenu comes available that allows you to use the cursors to isolate the part of the waveform that must be used for the integration process.

## APPENDICES

## Appendix A <br> MATHPLUS CURSORS menu

(Digital part only)


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